Online Partial Conditional Plan Synthesis for POMDPs with Safe-Reachability Objectives: Methods and Experiments

Yue Wang^{*}, Abdullah Al Redwan Newaz^{*}, Juan David Hernández^{**}, Swarat Chaudhuri and Lydia E. Kavraki

Abstract—The framework of Partially Observable Markov Decision Processes (POMDPs) offers a standard approach to model uncertainty in many robot tasks. Traditionally, POMDPs are formulated with optimality objectives. Here we study a different formulation of POMDPs with boolean objectives. For robotic domains that require a correctness guarantee of accomplishing tasks, boolean objectives are natural formulations. We investigate the problem of POMDPs with a common boolean objective: safereachability, requiring that the robot eventually reaches a goal state with a probability above a threshold while keeping the probability of visiting unsafe states below a different threshold. Our approach builds upon the previous work that represents POMDPs with boolean objectives using symbolic constraints. We employ a Satisfiability Modulo Theories (SMT) solver to efficiently search for solutions, i.e., policies or conditional plans that specify the action to take contingent on every possible event. A full policy or conditional plan is generally expensive to compute. To improve computational efficiency, we introduce the notion of partial conditional plans that cover sampled events to approximate a full conditional plan. Our approach constructs a partial conditional plan parameterized by a replanning probability. We prove that the failure rate of the constructed partial conditional plan is bounded by the replanning probability. Our approach allows users to specify an appropriate bound on the replanning probability to balance efficiency and correctness. Moreover, we update this bound properly to quickly detect if the current partial conditional plan meets the bound and avoid unnecessary computation. In addition, to further improve the efficiency, we cache partial conditional plans for sampled belief states and reuse these cached plans if possible. We validate our approach in several robotic domains. The results show that our approach outperforms a previous policy synthesis approach for POMDPs with safe-reachability objectives in these domains.

Note to Practitioners—This paper was motivated by two observations. On one hand, in robotics applications where uncertainty in sensing and actions is present, the solution to the classical POMDP formulation is expensive to compute in general. On the other hand, in certain practical scenarios, formulations other than the classical POMDP make a lot of sense and can provide flexibility in balancing efficiency and correctness. This paper considers a modified POMDP formulation that includes a boolean objective, namely safe-reachability. The paper uses the notion of a partial conditional plan. Rather than explicitly enumerating all possible observations to construct a full conditional plan, this work samples a subset of all observations to ensure bounded replanning probability. Our theoretical and empirical results show that the failure rate of the constructed partial conditional plan is

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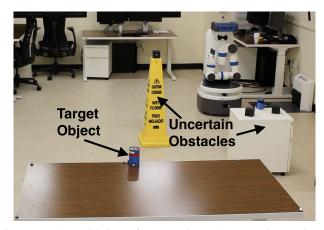


Fig. 1: A robot with imperfect actuation and perception navigates through an office to pick up the blue can on the table while avoiding collisions with uncertain obstacles such as floor signs and file cabinets.

bounded by the replanning probability. Moreover, these partial conditional plans can be cached to further improve performance. Our results suggest that for domains where replanning is easy, increasing the replanning probability bound usually leads to better scalability, and for domains where replanning is difficult or impossible in some states, we can decrease the bound and allocate more computation time to achieve a higher success rate. Hence, in certain cases, the practitioner can take advantage of their knowledge of the problem domain to scale to larger problems. Preliminary physical experiments suggest that this approach is applicable to real-world robotic domains but it requires a discrete representation of the workspace. How to deal with continuous workspace directly is an interesting future direction.

Index Terms—Robots, Uncertainty, Planning, POMDPs with Boolean Objectives, Safe-Reachability

I. INTRODUCTION

PLANNING robust executions under uncertainty, e.g., uncertain effects from imperfect controllers and sensors, is a fundamental concern in robotics. POMDPs [1] provide a standard framework for modeling many robot tasks under uncertainty. (e.g., [2]–[8]). The solutions to POMDPs are *policies* [1] or *conditional plans* [9] that specify the actions to take under *all possible* events during execution.

Traditionally, the goal of solving POMDPs is to find optimal solutions with respect to a quantitative objective such as that maximize (discounted) rewards [2], [3], [5], [9]–[14]. While this purely quantitative formulation is suitable for many applications,

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some robotic settings demand synthesis concerning boolean requirements. For example, consider a robot with imperfect actuation and perception working in an office environment with uncertain obstacles such as floor signs and furniture (Fig. 1). Due to uncertainty, the locations of the robot and the obstacles are partially observable, and the robot's action effects and observations are both probabilistic. In this probabilistic setting, a reasonable task requirement for the robot is to eventually pick up the target object with a probability above a threshold while keeping the probability of collision below a different threshold. This task requirement is naturally formulated as a boolean objective written in temporal logic. Moreover, formulating boolean requirements implicitly as quantitative objectives by assigning proper rewards for goal states and unsafe states does not always yield good solutions for certain domains [15]. Therefore, POMDPs with explicit boolean objectives are better formulations than quantitative POMDPs in these domains.

Policy synthesis for POMDPs with boolean objectives has been studied in previous works [4], [16]–[18], where the goal is to satisfy a temporal property with *probability 1* (almost-sure satisfaction). A more general policy synthesis for POMDPs with boolean objectives is to synthesize policies that satisfy a temporal property with *a probability above a threshold*. In this work, we study this problem for the special case of *safereachability* objectives, which require that with a probability above a threshold, a goal state is eventually reached while keeping the probability of visiting unsafe states below a different threshold. Many robot tasks such as the one in Fig. 1 can be formulated as a safe-reachability objective.

Our previous work [6] has presented a method called Bounded Policy Synthesis (BPS) for POMDPs with safereachability objectives. BPS computes a valid policy over the goal-constrained belief space rather than the entire belief space to improve efficiency. The goal-constrained belief space only contains beliefs visited by desired executions achieving the safe-reachability objective and is generally much smaller than the original belief space. BPS is an offline synthesis method that computes a full policy before execution. Another category of approaches to planning under uncertainty is online planning that interleaves planning and execution [5], [13], [14], [19]-[22]. Offline synthesis offers a strong correctness guarantee, but it is difficult to scale. Online planning is much more scalable and works well when replanning is likely to succeed, but it often fails when replanning is difficult or infeasible in some states, making it hard to ensure correctness.

In this work, our goal is to scale up our previous BPS method further through online planning. Specifically, we present a method called *Online Partial Conditional Plan Synthesis* (OPCPS) for POMDPs with safe-reachability objectives. OPCPS is based on the new notion of *partial conditional plans*, which only contains a sampled subset of all possible events and approximates a full policy. OPCPS computes a partial conditional plan parameterized by a *replanning probability*, i.e., the probability of encountering an event not covered by the partial conditional plan, thus requiring replanning. We offer a theoretical analysis of this framework, showing that the failure rate of the constructed partial conditional plan is bounded by the replanning probability. OPCPS allows users to specify an

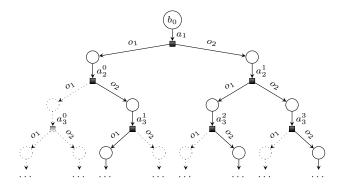


Fig. 2: A full conditional plan γ_k contains both solid and dotted branches. a_1, a_2^0, \ldots are actions. o_1 and o_2 are observations. A partial conditional plan γ_k^p contains only solid branches.

appropriate bound on the replanning probability to balance efficiency and correctness: for domains where replanning is likely to succeed, increasing the bound usually leads to better scalability, and for domains where replanning is difficult or impossible in some states, users can decrease the bound and allocate more time to achieve a higher success rate.

To further improve performance, OPCPS updates the replanning probability bound properly during the partial conditional plan construction. This bound update enables quicker detection of the current partial conditional plan meeting the bound and avoids unnecessary computation. For a better safety guarantee, OPCPS checks whether the successor belief of every uncovered observation of the constructed partial conditional plan satisfies the safety requirement. Thus OPCPS guarantees that the robot still satisfies the safety requirement when replanning fails. Section IV-B has more details on the bound update and the safety guarantee of OPCPS. What is more, we cache partial conditional plans for sampled belief states and reuse these plans if possible to avoid repetitive computation. In certain cases, as we explain in Section IV-C, caching partial conditional plans leads to increased computational efficiency.

We evaluate OPCPS in the kitchen domain presented in [6] and the Tag domain [3]. We also validate OPCPS on a Fetch robot for the domain shown in Fig. 1. The results demonstrate that OPCPS scales better than BPS and can solve problems that are beyond the capabilities of BPS within the time limit.

This paper is a significant extension of the preliminary findings presented in [23]. First, we extend the OPCPS algorithm presented in [23] with partial conditional plan caching. Second, we show that OPCPS with caching greatly improves running times in the experiments. Third, we conducted a physical experiment to validate OPCPS with the new caching option on a Fetch robot. Hence, the algorithms presented in this paper can be regarded as improved versions of the algorithms in [23].

II. RELATED WORK

The analysis of POMDPs can be divided into three categories. In the first category, the objective is to find optimal solutions concerning quantitative rewards. Many previous POMDP algorithms [3], [5], [9], [11]–[14] focus on maximizing (discounted) rewards. In the second category, the objective combines the quantitative rewards of the traditional POMDPs with notions of risk and cost. Recently, there has been a growing interest in constrained POMDPs [15], [24]-[26], chance-constrained POMDP [27], and risk-sensitive POMDPs [28], [29] that handle cost/risk constraints explicitly. The third category consists of POMDPs with high-level boolean requirements written in temporal logic. Some works [4], [16] have investigated almostsure satisfaction of POMDPs with temporal properties, where the goal is to check whether a given temporal property can be satisfied with probability 1. A more general policy synthesis problem of POMDPs with safe-reachability objectives has been introduced in our previous work [6]. It has been shown that for robotic domains that require a correctness guarantee of accomplishing tasks. POMDPs with safe-reachability provide a better guarantee of safety and reachability than the quantitative POMDP formulations [6].

While several works [30], [31] propose different types of reinforcement learning algorithms to address policy synthesis problems for MDP, to the best of our knowledge there are few works on policy synthesis based on reinforcement learning for POMDPs [32]. In recent work [33], the authors present macro-action discovery from a low-level POMDP model by chaining sequences of open-loop actions together with the task-specific value of information. In [34], the authors proposed a reinforcement learning-based POMDP solver for Autonomous Sequential Repair Problems. They use a neural network classifier for approximating successive policies. In [35], the authors model adaptive grasping using tactile and visual sensors as a POMDP problem and proposed a combination of the model-based POMDP planning and imitation learning to learn a robust strategy for grasping previously unseen objects.

In this work, we focus on POMDPs with safe-reachability objectives and evaluate our previous BPS approach [6]. While BPS synthesizes a full policy (conditional plan) offline that covers all possible events, our approach is an online method that interleaves the computation of a partial conditional plan and execution. Since a partial conditional plan only contains a sampled subset of all possible events, our method achieves better scalability than BPS and can solve problems that are beyond the capabilities of BPS within the time limit.

The idea of partial conditional plans resembles the stateof-the-art online POMDP algorithm based on Determinized Sparse Partially Observable Tree (DESPOT) [5], [13]. Both DESPOT and our partial conditional plans contain a subset of all possible observations to improve efficiency. There are two major differences between our method and DESPOT: first, DESPOT handles POMDPs with (discounted) rewards while our approach solves POMDPs with safe-reachability objectives. Second, DESPOT contains all action branches while our approach constructs partial conditional plans (Fig. 2) that only contains one action per step, which is part of the desired execution satisfying the safe-reachability objective.

III. PROBLEM FORMULATION

We follow the notation in [6] for POMDPs with safereachability objectives.

A. Partially Observable Markov Decision Process

Definition 1 (POMDP [1]). A POMDP is a tuple P = (S, A, T, O, Z), where S is a finite set of states, A is a finite set of actions, T is a probabilistic transition function, O is a finite set of observations, and Z is a probabilistic observation function. T(s, a, s') = Pr(s'|s, a) specifies the probability of moving to state $s' \in S$ after taking action $a \in A$ in state $s \in S$. Z(s', a, o) = Pr(o|s', a) specifies the probability of observing $o \in O$ after taking action $a \in A$ and reaching $s' \in S$.

Due to uncertainty, states are partially observable and typically we maintain a probability distribution (*belief*) over all states $b: S \mapsto [0, 1]$ with $\sum_{s \in S} b(s) = 1$. The set of all beliefs $\mathcal{B} = \{b: S \mapsto [0, 1] \mid \sum_{s \in S} b(s) = 1\}$ is the *belief space*.

The belief space transition function $\mathcal{T}_{\mathcal{B}}: \mathcal{B} \times \mathcal{A} \times \mathcal{O} \to \mathcal{B}$ is *deterministic*. $b_a^o = \mathcal{T}_{\mathcal{B}}(b, a, o)$ is the successor belief for a belief $b \in \mathcal{B}$ after taking an action $a \in \mathcal{A}$ and receiving an observation $o \in \mathcal{O}$, defined according to Bayes rule: $\forall s' \in \mathcal{S}, \ b_a^o(s') = \frac{\mathcal{Z}(s', a, o) \sum\limits_{s \in \mathcal{S}} \mathcal{T}(s, a, s')b(s)}{\Pr(o|b, a)}$, where $\Pr(o|b, a) = \sum\limits_{s' \in \mathcal{S}} \mathcal{Z}(s', a, o) \sum\limits_{s \in \mathcal{S}} \mathcal{T}(s, a, s')b(s)$ is the probability of receiving the observation o after taking the action ain the belief b.

Definition 2 (Plan). A k-step plan is a sequence $\sigma = (b_0, a_1, o_1, \ldots, a_k, o_k, b_k)$ such that for all $i \in (0, k]$, the belief updates satisfy the transition function $\mathcal{T}_{\mathcal{B}}$, i.e., $b_i = \mathcal{T}_{\mathcal{B}}(b_{i-1}, a_i, o_i)$, where $a_i \in \mathcal{A}$ is an action and $o_i \in \mathcal{O}$ is an observation.

B. Safe-Reachability Objective

In this work, we consider POMDPs with *safe-reachability* objectives:

Definition 3 (Safe-Reachability Objective). A safe-reachability objective is a tuple $\mathcal{G} = (Dest, Safe)$, where $Safe = \{b \in \mathcal{B} \mid \sum_{\substack{s \text{ violates safety} \\ s \text{ objective } safety}} b(s) < \delta_2\}$ is a set of safe beliefs and $Dest = \{b \in Safe \mid \sum_{\substack{s \text{ is a goal state} \\ s \text{ objective}}} b(s) > 1 - \delta_1\} \subseteq Safe$ is a set of goal beliefs. δ_1 and δ_2 are small values that represent tolerance.

A safe-reachability objective \mathcal{G} compactly represents the set $\Omega_{\mathcal{G}}$ of valid plans:

Definition 4 (Valid Plan). A k-step plan $\sigma = (b_0, a_1, o_1, \dots, a_k, o_k, b_k)$ is valid w.r.t. a safe-reachability objective $\mathcal{G} = (Dest, Safe)$ if b_k is a goal belief $(b_k \in Dest)$ and all beliefs visited before step k are safe beliefs $(\forall i \in [0, k), b_i \in Safe)$.

Note that the safety requirement in the safe-reachability objective only states that for every step of the plan, the probability of being in an unsafe state is within the threshold. This safety requirement does not necessarily extend to the safety of the whole plan, i.e., the probability of visiting an unsafe state is within the same threshold when executing the plan starting from the initial belief. To achieve the safety of the whole plan, we should consider the chance-constraints presented in [27], which is beyond the scope of this paper and a possible future extension of this work.

C. Solution to POMDPs with Safe-Reachability Objective

The solution to POMDPs with safe-reachability Objective is a *valid* policy that specifies the action to take contingent on all possible events:

Definition 5 (Valid Policy).

A valid policy $\pi : \mathcal{B} \to \mathcal{A}$ is a function that maps a belief $b \in \mathcal{B}$ to an action $a \in \mathcal{A}$. A policy π defines a set of plans in belief space: $\Omega_{\pi} = \{\sigma = (b_0, a_1, o_1, ...) \mid \forall i > 0, a_i = \pi(b_{i-1}) \text{ and } o_i \in \mathcal{O}\}$. For each plan $\sigma \in \Omega_{\pi}$, the action a_i at each step *i* is chosen by the policy π . For a valid policy, the set Ω_{π} of plans defined by the policy π are all valid plans.

D. Partial Conditional Plan

Computing an exact policy over the entire belief space \mathcal{B} is intractable, due to the curse of dimensionality [36]: \mathcal{B} is a high-dimensional space with an infinite number of beliefs. To make the problem tractable, we can exploit the *reachable belief space* \mathcal{B}_{b_0} [3], [11]. \mathcal{B}_{b_0} only contains beliefs reachable from the initial belief b_0 and is generally much smaller than \mathcal{B} . Therefore, instead of computing a policy $\pi : \mathcal{B} \mapsto \mathcal{A}$ over the entire belief space, we only compute a policy $\pi_{\mathcal{B}_{b_0}} : \mathcal{B}_{b_0} \mapsto \mathcal{A}$ over the reachable belief space.

Our previous BPS work [6] has shown that the performance of policy synthesis for POMDPs with safe-reachability objectives can be further improved based on the notion of a *goal-constrained belief space* $\mathcal{B}_{\mathcal{G}}$. $\mathcal{B}_{\mathcal{G}}$ combines the reachable belief space \mathcal{B}_{b_0} and the set $\Omega_{\mathcal{G}}$ of valid plans defined by the safe-reachability objective \mathcal{G} . $\mathcal{B}_{\mathcal{G}}$ only contains beliefs reachable from the initial belief b_0 under a valid plan $\sigma \in \Omega_{\mathcal{G}}$ and is generally much smaller than the reachable belief space \mathcal{B}_{b_0} .

Previous results [37]–[39] have shown that the problem of policy synthesis for POMDPs is generally undecidable. However, when restricted to a bounded horizon, this problem becomes PSPACE-complete [36], [40]. Therefore, BPS computes a bounded policy π over the goal-constrained belief space $\mathcal{B}_{\mathcal{G}}$ within a bounded horizon h, where the horizon (number of steps) of the policy is less than a given bound h. This bounded policy π is essentially a set of conditional plans [9]:

Definition 6 (Conditional Plan). A k-step conditional plan $\gamma_k \in \Gamma_k$ is a tuple $\gamma_k = (b, a, \nu_k)$, where $b \in \mathcal{B}$ is a belief, $a \in \mathcal{A}$ is an action and $\nu_k : \mathcal{O} \mapsto \Gamma_{k-1}$ is an observation strategy that maps an observation $o \in \mathcal{O}$ to a (k-1)-step conditional plan $\gamma_{k-1} = (b', a', \nu_{k-1}) \in \Gamma_{k-1}$, where $b' = \mathcal{T}_{\mathcal{B}}(b, a, o)$ is the successor belief.

Fig. 2 shows an example k-step conditional plan $\gamma_k = (b_0, a_1, \nu_k)$. γ_k defines a set Ω_{γ_k} of k-step plans $\sigma_k = (b_0, a_1, o_1, \dots, a_k, o_k, b_k)$. For each plan $\sigma_k \in \Omega_{\gamma_k}$, the action a_1 at step 1 is chosen by the k-step conditional plan γ_k , the action a_2 at step 2 is chosen by the (k-1)-step conditional plan $\gamma_{k-1} = \nu_k(o_1)$, ..., and the action a_k at step k is chosen by the one-step conditional plan $\gamma_1 = \nu_2(o_{k-1})$.

Definition 7 (Valid Conditional Plan). A k-step conditional plan γ_k is valid w.r.t. a safe-reachability objective \mathcal{G} if every plan in Ω_{γ_k} is valid ($\Omega_{\gamma_k} \subseteq \Omega_{\mathcal{G}}$).

It is clear that the number of valid plans in a valid k-step conditional plan γ_k grows exponentially as the horizon k increases. To address this challenge, our method computes *partial* conditional plans that only contains a small number of valid plans to approximate full conditional plans:

Definition 8 (Partial Conditional Plan). A *k-step* partial conditional plan is a tuple $\gamma_k^p = (b, a, \mathcal{O}_k^p, \nu_k^p)$, where $b \in \mathcal{B}$ is a belief, $a \in \mathcal{A}$ is an action, $\mathcal{O}_k^p \subseteq \mathcal{O}$ is a subset of the observation set \mathcal{O} , and $\nu_k^p : \mathcal{O}_k^p \mapsto \Gamma_{k-1}^p$ is a partial observation strategy that maps an observation $o \in \mathcal{O}_k^p$ to a (k-1)-step partial conditional plan $\gamma_{k-1}^p = (b', a', \mathcal{O}_{k-1}^p, \nu_{k-1}^p)$, where $b' = \mathcal{T}_{\mathcal{B}}(b, a, o)$ is the successor belief. When $\mathcal{O}_k^p = \mathcal{O}$, the partial conditional plan γ_k^p is a full conditional plan $\gamma_k \in \Gamma_k$. For k = 1, the observation strategy of γ_1^p is $\nu_1 = \emptyset$.

Similarly, a k-step partial conditional plan γ_k^p defines a set $\Omega_{\gamma_k^p}$ of k-step plans σ_k in belief space, and we can define a *valid* partial conditional plan:

Definition 9 (Valid Partial Conditional Plan). A k-step partial conditional plan γ_k^p is valid w.r.t. a safe-reachability objective \mathcal{G} if every plan in $\Omega_{\gamma_k^p}$ is valid.

E. Replanning Probability

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Since a partial conditional plan $\gamma_k^p = (b, a, \mathcal{O}_k^p, \nu_k^p)$ only contains a subset of all observation branches at each step (see Fig. 2), during online execution, it is possible that an observation branch $o \in \mathcal{O} - \mathcal{O}_k^p$ that is not part of the partial conditional plan is visited. In this case, we need to recursively compute a new partial conditional plan for this new branch o. However, since γ_k^p does not consider all possible observation branches, it is possible that the action chosen by γ_k^p is *invalid* for the new observation branch o, even for a valid partial conditional plan. As a result, there are no partial conditional plans for the new observation branch o and execution fails.

To preserve correctness, we would like to bound the *failure* rate $p_{\text{fail}}(\gamma_k^p) = \Pr(\text{failure}|\gamma_k^p)$ measured under a valid partial conditional $\gamma_k^p = (b, a, \mathcal{O}_k^p, \nu_k^p)$. However, computing p_{fail} is costly because it requires checking whether the action *a* chosen by γ_k^p is valid for every uncovered observation branch $o \in \mathcal{O} - \mathcal{O}_k^p$, which essentially computes a *full* conditional plan. Alternatively, we can easily compute the *replanning probability* $p_{\text{replan}}(\gamma_k^p) = \Pr(\text{replanning}|\gamma_k^p)$ of reaching an uncovered observation branch $o \in \mathcal{O} - \mathcal{O}_k^p$ and requiring *replanning*:

$$p_{\text{replan}}(\gamma_k^p) = \sum_{o \in \mathcal{O}_k^p} \Pr(o|b, a) p_{\text{replan}}(\nu_k^p(o)) + \sum_{o \in \mathcal{O} - \mathcal{O}_k^p} \Pr(o|b, a)$$
(1)

For the base case k = 1, $p_{\text{replan}}(\gamma_1^p) = \sum_{o \in \mathcal{O} - \mathcal{O}_1^p} \Pr(o|b, a)$.

The following theorem states that for a *valid* partial conditional plan γ_k^p , the failure rate $p_{\text{fail}}(\gamma_k^p)$ is bounded by the replanning probability $p_{\text{replan}}(\gamma_k^p)$:

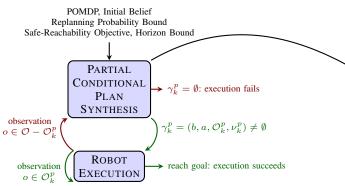


Fig. 3: The overall structure of the OPCPS Algorithm

Theorem 1. For any valid partial conditional plan γ_k^p , $p_{fail}(\gamma_k^p) \leq p_{replan}(\gamma_k^p)$.

Proof. We prove Theorem 1 by induction. First, we define $\delta_{\text{fail}}(b) : \mathcal{B} \mapsto \{0, 1\}$ as an indicator, and when $\delta_{\text{fail}}(b) = 1$, there are no valid partial conditional plans for belief *b* and execution fails.

• Base case (k = 1): Since $\gamma_1^p = (b, a, \mathcal{O}_1^p, \emptyset)$ is valid, for every covered observation $o \in \mathcal{O}_1^p$, $b' = \mathcal{T}_{\mathcal{B}}(b, a, o) \in$ *Dest* is the terminal goal belief and thus $\delta_{\text{fail}}(b') = 0$. Therefore,

$$p_{\text{fail}}(\gamma_1^p) = \sum_{o \in \mathcal{O} - \mathcal{O}_1^p} \Pr(o|b, a) \delta_{\text{fail}}(b')$$
$$\leq \sum_{o \in \mathcal{O} - \mathcal{O}_1^p} \Pr(o|b, a) = p_{\text{replan}}(\gamma_1^p)$$

since $\delta_{\text{fail}}(b') \leq 1$ where $b' = \mathcal{T}_{\mathcal{B}}(b, a, o)$ is the successor belief for the uncovered observation $o \in \mathcal{O} - \mathcal{O}_1^p$.

Inductive case (k > 1): Since γ^p_k = (b, a, O^p_k, ν^p_k) is valid, for every covered observation o ∈ O^p_k, the corresponding (k - 1)-step partial conditional plan ν^p_k(o) is also valid. Assume p_{fail}(ν^p_k(o)) ≤ p_{replan}(ν^p_k(o)), then

$$p_{\text{fail}}(\gamma_k^p) = \sum_{o \in \mathcal{O}_k^p} \Pr(o|b, a) p_{\text{fail}}(\nu_k^p(o)) + \sum_{o \in \mathcal{O} - \mathcal{O}_k^p} \Pr(o|b, a) \delta_{\text{fail}}(b') \leq \sum_{o \in \mathcal{O}_k^p} \Pr(o|b, a) p_{\text{replan}}(\nu_k^p(o)) + \sum_{o \in \mathcal{O} - \mathcal{O}_k^p} \Pr(o|b, a) = p_{\text{replan}}(\gamma_k^p)$$

since $\delta_{\text{fail}}(b') \leq 1$ where $b' = \mathcal{T}_{\mathcal{B}}(b, a, o)$ is the successor belief for the uncovered observation $o \in \mathcal{O} - \mathcal{O}_k^p$.

Therefore, For any k-step valid partial conditional plan $\gamma_k^p = (b, a, \mathcal{O}_k^p, \nu_k^p), \ p_{\text{fail}}(\gamma_k^p) \leq p_{\text{replan}}(\gamma_k^p).$

F. Problem Statement

Given a POMDP P, an initial belief b_0 , a replanning probability bound $\delta_{p_{\text{replan}}}$, a safe-reachability objective \mathcal{G} and a horizon bound h, our goal is to synthesize a valid k-step

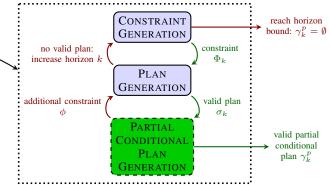


Fig. 4: The component of Partial conditional plan synthesis in Fig. 3

Algorithm 1: OPCPS

Input: POMDP P = (S, A, T, O, Z), Initial Belief b_{init} , Replanning Probability Bound $\delta_{p_{\text{replan}}}$, Safe-Reachability Objective $\mathcal{G} = (Dest, Safe)$, Horizon Bound h Output: A boolean: true - success, false - failure /* Generate the partial conditional plan */ 1 $\gamma_k^p \leftarrow \text{PartialContionalPlanSynthesis}(P, b_{init}, \mathcal{G}, \delta_{p_{\text{replan}}}, h)$ 2 if $\gamma_k^p = \emptyset$ then /* No partial conditional plans: failure */ $return \ {\rm false}$ 3 4 repeat $(a, \mathcal{O}_k^p, \nu_k^p) \leftarrow \gamma_k^p$ 5 Execute action a 6 Receive observation o 7 $b_{init} \leftarrow \mathcal{T}_{\mathcal{B}}(b_{init}, a, o)$ 8 /* Update belief */ if $b_{init} \in Dest$ then 9 /* reach a goal belief: success */ return true 10 /* Get the next partial conditional plan $\gamma_k^p \leftarrow \nu_k^p(o)$ 11 $h \leftarrow h -$ 12 /* Reduce the horizon bound */ 13 until $\gamma_k^p = \emptyset$ /* recursively perform OPCPS on new branch 14 return OPCPS(P, b_{init} , G, h)

 $(k \leq h)$ partial conditional plan $\gamma_k^p = (b_0, a, \mathcal{O}_k^p, \nu_k^p)$ with a replanning probability $p_{\text{replan}}(\gamma_k^p) \leq \delta_{p_{\text{replan}}}$.

Since the replanning probability $p_{\text{replan}}(\gamma_k^p)$ is bounded by $\delta_{p_{\text{replan}}}$, by Theorem 1, γ_k^p guarantees achieving the given safereachability objective with a probability at least $1 - \delta_{p_{\text{replan}}}$. Note that when $p_{\text{replan}}(\gamma_k^p) = 0$, γ_k^p is a full conditional plan.

IV. ONLINE PARTIAL CONDITIONAL PLAN SYNTHESIS

Fig. 3 shows the overall structure of OPCPS (Algorithm 1). OPCPS follows the typical online planning paradigm [41] that interleaves synthesis of valid partial conditional plans (line 1) and execution (lines 6, 7, 8). If there are no valid partial conditional plans within the horizon bound (line 2), execution fails. Otherwise, OPCPS follows the generated partial conditional plan until a goal belief is reached (line 9: execution succeeds) or a new observation $o \in \mathcal{O} - \mathcal{O}_k^p$ is received (line 13). In the latter case, OPCPS recursively replans for the observation o. Next, we describe the partial conditional plan synthesis algorithm (Fig. 4) used in OPCPS.

	orithm 2: PartialConditionalPlanSynthesis
In	put: POMDP P, Initial Belief b_{init} , Replanning Probability Pound δ
	Bound $\delta_{p_{\text{replan}}}$, Safe-Reachability Objective $\mathcal{G} = (Dest, Safe)$, Horizon Bound h
0	utput: Valid partial conditional plan γ_k^p with
	$p_{\text{replan}}(b_{init}, \gamma_k^p) \le \delta_{p_{\text{replan}}}$
/*	Φ_k is the constraint to symbolically encode
	the goal-constrained belief space */
	$_k \leftarrow (b_0 = b_{init})$ /* Start from initial belief */
6 k	$\leftarrow 0$ /* k is the number of steps */
7 W	hile $k \leq h$ do
	/* Add transition at step k if $k > 0$ */
8	if $k > 0$ then
9	
20	$\operatorname{push}(\Phi_k)$ /* Push scope */
	/* Add goal constraints at step k */
1	$\Phi_k \leftarrow \Phi_k \land G(\sigma_k, \mathcal{G}, k)$
2	repeat
	/* Plan generation: check satisfiability
	of Φ_k via an SMT solver [42] */
3	$\sigma_k \leftarrow \text{IncrementalSMT}(\Phi_k)$
4	if $\sigma_k \neq \emptyset$ then /* Find valid plan */
-	/* Generate partial conditional plan */
5	$\gamma_k^p, \phi = \text{PartialConditionalPlanGeneration}(P, \delta)$
	$\begin{split} \delta_{\mathcal{P}_{\text{replan}}}, \mathcal{G}, \sigma_k, 1, k) \\ \mathbf{if} \ \emptyset = \gamma_k^p \ \mathbf{then} \ / \star \ \text{Generation failed} \qquad \star / \end{split}$
6	if $\emptyset = \gamma_k^r$ then /* Generation failed */ /* Blocking invalid plans */
7	$\Phi_k \leftarrow \Phi_k \land \phi$
28	else
29	$\begin{bmatrix} & \\ & \\ & \\ & \end{bmatrix} return \ \gamma^p_k$
0	until $\sigma_k = \emptyset$
1	$\operatorname{pop}(\Phi_k)$ /* Pop goal and ϕ at step k */
2	$k \leftarrow k+1$ /* Increase the horizon */
3 re	- turn Ø

A. Partial Conditional Plan Synthesis

In partial conditional plan synthesis (Fig. 4 and Algorithm 2) we replace the policy generation component in BPS [6] with a new partial conditional plan generation (the green dashed component). For completeness, we offer a brief summary of the constraint generation and plan generation components in BPS. See [6] for more details.

In constraint generation (Fig. 4), given a POMDP P, an initial belief b_0 and a safe-reachability objective $\mathcal{G} = (Dest, Safe)$, we first construct a constraint Φ_k to symbolically encode the goal-constrained belief space over a bounded horizon k based on the encoding from Bounded Model Checking [43] (line 15, 19, 21). Φ_k compactly represents the requirement of reaching a goal belief $b \in Dest$ safely in k steps. In constraint generation (Fig. 4), we use the Bounded Model Checking [43] encoding to construct Φ_k , which contains three parts:

- 1) start from the initial belief (line 15) : $b_0 = b_{init}$.
- 2) unfold the transition up to horizon k (line 19): $\bigwedge_{i=1}^{\kappa} (b_i = \mathcal{T}_{\mathcal{B}}(b_{i-1}, a_i, o_i)).$
- 3) satisfy the objective \mathcal{G} (line 21): $G(\sigma_k, \mathcal{G}, k) = \bigvee_{i=0}^k (b_i \in Dest \land (\bigwedge_{j=0}^{i-1} (b_j \in Safe))).$

Then in plan generation (Fig. 4), we compute a valid *plan* σ_k by checking the satisfiability of Φ_k (line 23) through an SMT solver [42]. Note that the horizon k restricts the plan

Algorithm 3: PartialConditionalPlanGeneration Input: POMDP P = (S, A, T, O, Z), Replanning Probability Bound $\delta_{p_{replan}}$, Safe-Reachability Objective $\mathcal{G} = (Dest, Safe)$, Valid k-Step Plan $\sigma_k = (b_0^{\sigma_k}, a_1^{\sigma_k}, a_1^{\sigma_k}, \dots, b_k^{\sigma_k})$, Step *i*, Horizon Bound *h* Output: Valid partial conditional plan γ_k^p with replanning probability $p_{replan}(\gamma_k^p) \leq \delta_{p_{replan}}$, Constraint ϕ for

blocking invalid plans 34 if i > k then /* Reach the last step k*/ /* Terminal belief: γ^p_k specifies nothing */ $\begin{bmatrix} \gamma_k^p \leftarrow (b_k^{\sigma_k}, \emptyset, \emptyset, \emptyset) \\ \mathbf{return} \ \gamma_k^p, \emptyset \end{bmatrix}$ 35 36 /* Initialize */ $\begin{array}{l} \textbf{37} \hspace{0.1cm} \mathcal{O}_{k}^{p} \leftarrow \emptyset, \hspace{0.1cm} \delta_{p_{\text{replan}}}^{\prime} \leftarrow \delta_{p_{\text{replan}}}, \hspace{0.1cm} b \leftarrow b_{i-1}^{\sigma_{k}}, \hspace{0.1cm} a \leftarrow a_{i}^{\sigma_{k}}, \hspace{0.1cm} o^{\prime} \leftarrow o_{i}^{\sigma_{k}} \\ / \star \hspace{0.1cm} \text{Recursively process next step} \end{array}$ */ 38 $\gamma_{\text{next}}^{p} \leftarrow$ PartialConditionalPlanGeneration $(P, \delta'_{p_{\text{replan}}}, \mathcal{G}, \sigma_k, i+1, h)$ 39 if $\gamma_{next}^p = \emptyset$ then /* Construction failed */ Construct ϕ using Formula 2, return \emptyset , ϕ */ 42 while $p_{replan}(\gamma_k^p) > \delta_{p_{replan}}$ do /* Bound update */ $\delta'_{p_{\text{replan}}} \leftarrow \delta'_{p_{\text{replan}}} + \frac{\Pr(o'|b,a)(\delta'_{p_{\text{replan}}} - p_{\text{replan}}(\nu_{k}^{p}(o'))}{\sum\limits_{o \in \mathcal{O} - \mathcal{O}_{k}^{p} - \{o'\}} \Pr(o|b,a)}$ 43 $o' \leftarrow$ sampled observation in $\mathcal{O} - \mathcal{O}_k^p$ based on the 44 probability of occurrence $b' \leftarrow \mathcal{T}_{\mathcal{B}}(b, a, o')$ /* Get new initial belief */ 45 if $b' \in \mathbb{M}$ then 46 /* Check the cache $\mathbb M$ 47 else 48 /* Recursively construct a next-step partial conditional plan */ 49 $\gamma_{\text{next}}^p \leftarrow$ PartialConditionalPlanSynthesis $(P, b', \delta'_{p_{replan}}, \mathcal{G}, i, h)$ /* Update the cache $\mathbb{M}(b') \leftarrow \gamma_{\text{next}}^p$ 50 if $\gamma_{next}^p = \emptyset$ then 51 /* Construction failed */ Construct ϕ using Formula 2, return \emptyset , ϕ 52 $\mathcal{O}^p_k \leftarrow \mathcal{O}^p_k \cup \{o'\}, \, \nu^p_k(o') \leftarrow \gamma^p_{\mathrm{next}} \quad \text{ /* Add } o' \text{ to } \gamma^p_k$ 53 */ /* Final safety check */ 54 foreach observation $o \in \mathcal{O} - \mathcal{O}_k^p$ do $b' \leftarrow \mathcal{T}_{\mathcal{B}}(b, a, o)$ 55 /* Try observation o */ 56 if $b' \notin Safe$ then /* Violates safety Construct ϕ using Formula 2, **return** \emptyset , ϕ 57 58 return γ_k^p, \emptyset

length and thus the robot can only execute k actions before reaching a goal belief $b \in Dest$.

If Φ_k is satisfiable, the SMT solver returns a valid plan $\sigma_k = (b_0^{\sigma_k}, a_1^{\sigma_k}, o_1^{\sigma_k}, \dots, b_k^{\sigma_k})$. This valid plan σ_k only covers a particular observation $o_i^{\sigma_k}$ at step *i*. In partial conditional plan generation (Fig. 4), we generate a valid partial conditional plan γ_k^p with a replanning probability $p_{\text{replan}}(\gamma_k^p) \leq \delta_{p_{\text{replan}}}$ (line 25) from this valid plan σ_k by sampling a subset $\mathcal{O}_k^p \subseteq \mathcal{O}$ of observations (solid branches in Fig. 2) at each step, where $\delta_{p_{\text{replan}}}$ is the given replanning probability bound. If this partial conditional plan generation fails, we construct an additional constraint ϕ to block invalid plans (line 27) and force the SMT solver to generate another better plan. Note that ϕ is only valid

for current horizon k and when we increase the horizon, we should *pop* the scope related to the additional constraints ϕ from the stack of the SMT solver (line 31) so that we can revisit σ_k with the increased horizon. The incremental SMT solver can efficiently generate alternate valid plans by maintaining a stack of scopes for the "knowledge" learned from previous satisfiability checks [6], [42], [44].

If Φ_k is unsatisfiable and there is no valid plan for the current horizon, we increase the horizon (line 32) and repeat the above steps until a valid partial conditional plan is found (line 29) or a given horizon bound is reached (line 17). Next, we describe the new partial conditional plan generation component.

B. Partial Conditional Plan Generation

In partial conditional plan generation (Algorithm 3), we construct a valid partial conditional plan γ_k^p that satisfies the given bound $\delta_{p_{\text{replan}}}$ from a valid plan σ_k . For each step *i*, we first recursively construct a next-step conditional plan γ_{next}^p for $o_i^{\sigma_k}$ (line 38). If the replanning probability $p_{\text{replan}}(\gamma_k^p)$ is greater than the bound $\delta_{p_{\text{replan}}}$ (line 42), we add more observation branches to γ_k^p by sampling a new observation o' according to the probability of occurrence (line 44) and recursively constructing a next-step partial conditional plan γ_{next}^p for o' (line 49). This is another partial conditional plan synthesis problem with a new initial belief b' (line 45), and can be solved recursively using Algorithm 2 shown in Fig. 4.

If we successfully construct a valid γ_{next}^p for o', we add o'to γ_k^p (line 41 or 53). Otherwise, this input plan σ_k cannot be an element of a *valid* partial conditional plan γ_k^p ($\sigma_k \notin \Omega_{\gamma_k^p}$). Therefore, the prefix $(b_0^{\sigma_k}, a_1^{\sigma_k}, o_1^{\sigma_k}, \dots, b_{i-1}^{\sigma_k}, a_i^{\sigma_k})$ of the input plan σ_k is invalid for the current horizon k and we construct the following additional constraint ϕ to block invalid plans:

$$\neg((b_0 = b_0^{\sigma_k}) \land (a_i = a_i^{\sigma_k}))$$
$$\land (\bigwedge_{m=1}^{i-1} (a_m = a_m^{\sigma_k}) \land (o_m = o_m^{\sigma_k}) \land (b_m = b_m^{\sigma_k})))$$
(2)

 ϕ blocks the invalid plans that have this prefix and avoids unnecessary checks of these plans (checking σ_k has already shown that these plans are invalid).

1) Updating Replanning Probability Bound: As we add more observation branches to the current partial conditional plan $\gamma_k^p = (b, a, \mathcal{O}_k^p, \nu_k^p)$, we update the replanning probability bound $\delta'_{p_{\text{replan}}}$ (line 43) for the remaining uncovered observation branches $\mathcal{O} - \mathcal{O}_k^p$ to avoid unnecessary computation.

Initially, \mathcal{O}_k^p is empty and $\delta'_{p_{\text{replan}}}$ is the input bound $\delta_{p_{\text{replan}}}$ (line 37). $\delta'_{p_{\text{replan}}}$ bounds the replanning probability $p_{\text{replan}}(\nu_k^p(o))$ of the next-step partial conditional plan $\nu_k^p(o)$ for every remaining the next-step partial conditional plan $\nu_{k}^{c}(o)$ for every remaining uncovered observation $o \in \mathcal{O} - \mathcal{O}_{k}^{p}$. $\delta'_{p_{replan}}$ guarantees that the replanning probability $p_{replan}(\gamma_{k}^{p})$ satisfies the original bound $\delta_{p_{replan}}$, i.e., $p_{replan}(\gamma_{k}^{p}) = \sum_{o \in \mathcal{O}} \Pr(o|b, a) p_{replan}(\nu_{k}^{p}(o)) \leq$ $\sum_{o \in \mathcal{O}} \Pr(o|b, a) \delta'_{p_{replan}} \leq \delta'_{p_{replan}} = \delta_{p_{replan}}$ since $p_{replan}(\nu_{k}^{p}(o)) \leq$ $\delta'_{p_{replan}}$ based on the definition of $\delta'_{p_{replan}}$. During partial conditional plan generation, after adding a new observation $o' \in \mathcal{O} - \mathcal{O}^{p}$ to the partial conditional

a new observation $o' \in \mathcal{O} - \mathcal{O}_k^p$ to the partial conditional

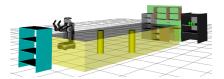


Fig. 5: The kitchen domain [6]: a robot navigates through the kitchen to pick up a green cup from the black storage area (reachability), while avoiding collisions with uncertain obstacles (e.g., chairs) modeled as cylinders placed in the yellow "shadow" region (safety).

plan γ_k^p (line 41 or 53), we update $\delta'_{p_{\rm replan}}$ to avoid unnecessary computation. Suppose we construct a new nextstep partial conditional plan γ_{next}^p with the same replanning probability α for every remaining uncovered observation $o \in \mathcal{O} - \mathcal{O}_k^p - \{o'\}$. Then the replanning probability of the observation branches $\mathcal{O} - \mathcal{O}_{k}^{p}$ is $\Pr(o'|b, a)p_{\text{replan}}(\nu_{k}^{p}(o')) + \alpha \sum_{o \in \mathcal{O} - \mathcal{O}_{k}^{p} - \{o'\}} \Pr(o|b, a) \leq \sum_{o \in \mathcal{O} - \mathcal{O}_{k}^{p}} \Pr(o|b, a)\delta'_{p_{\text{replan}}}$. There-fore $\alpha \leq \delta'_{p_{\text{replan}}} + \frac{\Pr(o'|b,a)(\delta'_{p_{\text{replan}}} - p_{\text{replan}}(\nu_{k}^{p}(o')))}{\sum_{o \in \mathcal{O} - \mathcal{O}_{k}^{p} - \{o'\}}}$. Then the new

bound for the remaining uncovered observation $o \in \mathcal{O} - \mathcal{O}_k^p - \{o'\}$ should be $\delta'_{p_{\text{replan}}} + \frac{\Pr(o'|b,a)(\delta'_{p_{\text{replan}}} - p_{\text{replan}}(\nu_k^p(o'))}{\sum\limits_{o \in \mathcal{O} - \mathcal{O}_k^p - \{o'\}} \Pr(o|b,a)}$ and this new

bound is at least $\delta'_{p_{\text{replan}}}$ since $p_{\text{replan}}(\nu^p_k(o')) \leq \delta'_{p_{\text{replan}}}$ according to the definition of $\delta'_{p_{\text{replan}}}$. When the replanning probability bound becomes larger, computing a partial conditional plan is usually less expensive. Therefore, updating the replanning probability bound (line 43) usually improves efficiency and still makes the current partial conditional plan γ_k^p satisfy the original bound $\delta_{p_{\text{renlan}}}$.

2) Safety Guarantee: After we construct a valid partial conditional plan $\gamma_k^p = (b, a, \mathcal{O}_k^p, \nu_k^p)$, if the uncovered observation set is not empty $(\mathcal{O} - \mathcal{O}_k^p \neq \emptyset)$, then the replanning probability $p_{\text{replan}}(\gamma_k^p) > 0$. Though this replanning probability is bounded by the given bound $\delta_{p_{\text{replan}}}$ and by Theorem 1, we know that the execution failure rate $p_{\text{fail}}(\gamma_k^p)$ is also bounded by $\delta_{p_{\text{replan}}}$. However, if $p_{\text{replan}}(\gamma_k^p) > 0$, during execution the robot might receive an uncovered observation $o \in \mathcal{O} - \mathcal{O}_k^p$ and there are no valid partial conditional plans for this observation o. Then execution fails due to unsuccessful replanning. In this case, though we cannot achieve the safe-reachability objective, a guarantee of the robot still satisfying the safety requirement is preferable to the situation where the robot violates the safety requirement. Our approach OPCPS can provide this safety guarantee by checking whether the successor belief of every uncovered observation $o \in \mathcal{O} - \mathcal{O}_k^p$ of the constructed partial conditional plan γ_k^p is a *safe* belief (lines 54-57).

C. Caching

The algorithm we have discussed so far recursively constructs a partial conditional plan for every sampled belief state. In some cases, those sampled beliefs are revisited under similar kstep plans starting from the initial belief. For instance, different invalid k-step plans can lead to the same belief state that violates our safety requirement. The original OPCPS presented in [23] does not cache partial conditional plans for sampled belief

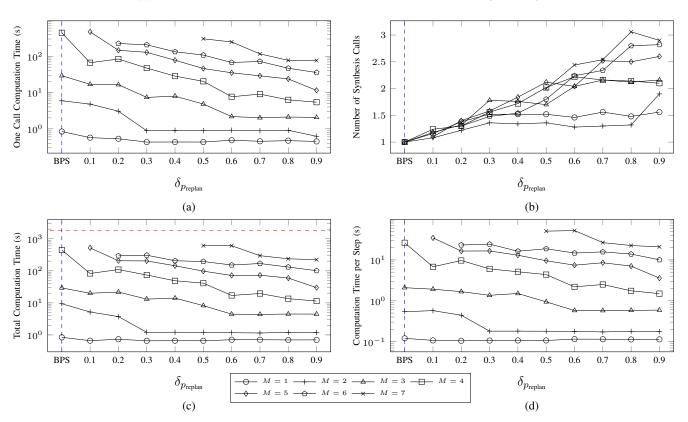


Fig. 6: Performance results for the kitchen domain as the bound $\delta_{p_{replan}}$ increases. Different plots correspond to tests with different numbers M of obstacles. Missing data points in a plot indicate time-out. The red dashed line is the plot of time = 1800 seconds (time-out). The blue dashed line passes through the data points generated by BPS. All the results are averaged over 50 independent runs.

states, resulting in repetitive computation of partial conditional plans for revisited belief states. Computing partial conditional plans requires invoking the incremental SMT solver, which is typically quite expensive. Therefore, it is more efficient to reuse previous computed partial conditional plans rather than constructing a new one from scratch. Moreover, for revisited belief states that violate the safety constraints and thus correspond to the empty partial conditional plan ϕ , caching also helps quickly invalidate the plans since we cached the empty partial conditional plan ϕ for these invalid beliefs.

Algorithm 3 augments the corresponding procedure from [23] with caching. For every sampled belief state, we first check whether this belief state is in the cache (line 46). In this work, we are focusing on *discrete* POMDPs and the belief state specifies the probability for each discrete state, which can be represented as a finite vector. When checking whether a belief state is in the cache, we are checking whether the belief state matches any belief state in the cache, i.e., we compare finite vectors. If we find this belief state in the cache, we can reuse the previous computed partial conditional plan (line 47). Otherwise, we compute a partial conditional plan for this belief state as in the previous OPCPS (line 49). Then we cache the new partial conditional plans for this sampled belief state (line 50). One can argue that in a large belief space caching each sampled belief might not be a feasible approach. However, we are dealing with the goal constrained belief space $\mathcal{B}_{\mathcal{G}}$, which is generally much smaller than the reachable belief space \mathcal{B}_{b_0} . In our case, the lack of caching previously computed

partial conditional plan leads to a slower convergence rate. To provide some intuitions, consider an invalid plan where there is a constraint violation near the goal belief but far from the initial belief. The incremental SMT solver dodges this violation by slightly modifying the k-step plan. In this case, the new k-step plan does not change drastically compared to the previous invalid plan. When not caching the previous solution conditional plans, OPCPS will spend a lot of time to recursively compute a new partial conditional plan at each planning step. It is reasonable to recursively compute a partial conditional plan in very dynamic or adversarial environments where one can observe constraint violation in each planning step. However, in many applications, the environment is mostly static and it is more efficient to reuse a previous solution rather than constructing a new one from scratch.

D. Algorithm Complexity

In the worst case, OPCPS will generate a full conditional plan (policy) and requires $O(I|\mathcal{O}|^h)$ calls to the SMT solver similar to BPS [6], where *I* is the number of interactions between plan generation and partial conditional plan generation, $|\mathcal{O}|$ is the size of observation set \mathcal{O} respectively and *h* is the horizon bound. In general cases, OPCPS can achieve a much better practical performance compared to BPS, thanks to the carefully designed *partial* conditional plan generation with replanning probability bound update and caching.

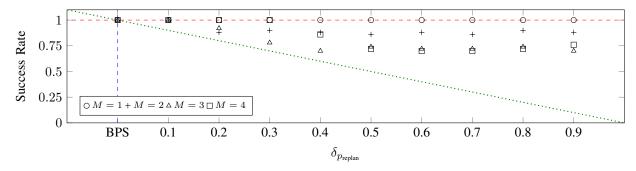


Fig. 7: Success rate as $\delta_{p_{replan}}$ increases. The green dotted line shows the plot of success rate = $1.0 - \delta_{p_{replan}}$. The red dashed line is the plot of success rate = 1.0. The blue dashed line passes through the data points generated by BPS.

V. EXPERIMENTS

We test OPCPS on the kitchen domain (horizon bound h = 30) presented in [6] and the classic Tag domain [3] (h = 100). We use Z3 [42] as our backend SMT solver. All experiments were conducted on a 3.0 GHz Intel[®] processor with 32 GB of memory. We set the time-out to be 1800 seconds. For all the tests of the kitchen and Tag domains, the results are averaged over 50 independent runs.

In a kitchen domain [6] (Fig. 5), a robot needs to eventually pick up a cup from the storage while avoiding collisions with M uncertain obstacles. This kitchen domain is an example scenario that requires a correctness guarantee of accomplishing tasks, and POMDPs with safe-reachability objectives provide a better correctness guarantee than the traditional quantitative POMDP formulations [6].

The kitchen environment is discretized into N = 36 regions. The actuation and perception of the robot are imperfect, modeled as ten uncertain robot actions: *move* and *look* in four directions, pick-up using the left or right hand. We assume that the robot starts at a known initial location. However, due to the robot's imperfect perception, the location of the robot and the locations of obstacles are all partially observable during execution. This kitchen domain has a large state space $|S| = C(N, M) \cdot N$, where C(N, M) is the number of *M*combinations from the set of N regions. In the largest test (M = 7) there are more than 10^8 states. See [6] for more details regarding the kitchen domain POMDP setup. We also validate the presented approach on a Fetch robot [45].

A. Performance

We evaluate our previous BPS method [6] and OPCPS (with the replanning probability bound $\delta_{p_{\text{replan}}}$ ranging from 0.1 to 0.9) in the kitchen domain with various numbers of obstacles. BPS computes a full conditional plan that covers all observation branches and is equivalent to OPCPS with $\delta_{p_{\text{replan}}} = 0$.

Fig. 6a, 6b, 6c and 6d show the average computation time of one synthesis call, the average number of synthesis calls, the average total computation time and the average computation time per step as the bound $\delta_{p_{replan}}$ increases, respectively. As shown in Fig. 6a (semi-log scale) and 6b, the computation time of one synthesis call decreases very quickly while the number of calls to partial conditional plan synthesis (Fig. 6b) does not increase much as $\delta_{p_{replan}}$ increases. Therefore, the total

computation time (Fig. 6c) keeps decreasing as $\delta_{p_{replan}}$ increases. Additionally, as we can see from Fig. 6c (semi-log scale), BPS can only scale up to 4 obstacles within 1800 seconds while OPCPS with replanning probability bound $\delta_{p_{\text{replan}}} = 0.9$ can scale up to 7 obstacles. With a small bound $\delta_{p_{\text{replan}}} = 0.1$, we observe a big performance gain compared to BPS: for the test case with M = 4 obstacles, the speedup is around 5 times and for the test case with M = 5 obstacles, BPS times out while OPCPS with $\delta_{p_{\text{replan}}} = 0.1$ can solve this test in around 9 minutes. Therefore, OPCPS achieves better performance than BPS in the tests by computing *partial* conditional plans to approximate *full* conditional plans. The results of the average computation time per step (Fig. 6d) also show the same trend. These results suggest that for domains where replanning is easy, increasing the replanning probability bound usually leads to better scalability.

B. Success Rate

For all the previous performance tests, the constructed partial conditional plans by OPCPS with different bounds $\delta_{p_{\text{replan}}}$ always achieve the safe-reachability objective (success rate = 100%) because the robot can move in four directions. When the robot enters a region surrounded by obstacles in three directions, the robot can always move back to its previous position, which means replanning is always possible. However, in some domains such as autonomous driving and robot chefs, when the robot commits to an action and finds something wrong, it is difficult or impossible to reverse the action effects and replan. To evaluate how OPCPS performs in these scenarios, we test OPCPS in the kitchen domain with different numbers M of obstacles (M < 4 since BPS times out for tests with more than four obstacles), but we disable the robot's move-north action. Therefore, when the robot performs move-south and enters a region surrounded by obstacles in three directions, replanning fails. However, the robot still satisfies the safety requirement, thanks to the safety guarantee of OPCPS.

Fig. 7 shows the success rate as the bound $\delta_{p_{\text{replan}}}$ increases. For all the tests, the success rate is always greater than $1.0 - \delta_{p_{\text{replan}}}$ (all data points are above the plot of success rate = $1.0 - \delta_{p_{\text{replan}}}$). This matches Theorem 1: the failure rate of a valid partial conditional plan is bounded by the replanning probability. Moreover, as the bound $\delta_{p_{\text{replan}}}$ decreases to 0, OPCPS produces a valid full conditional plan with 100% success rate. These results suggest that for some domains where we anticipate that

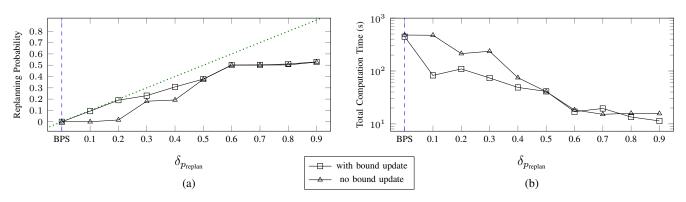


Fig. 8: Replanning probability and total computation time as the bound $\delta_{p_{\text{replan}}}$ increases (M = 4). The green dotted line shows the plot of replanning probability = $\delta_{p_{\text{replan}}}$. The blue dashed line passes through the data points generated by BPS.

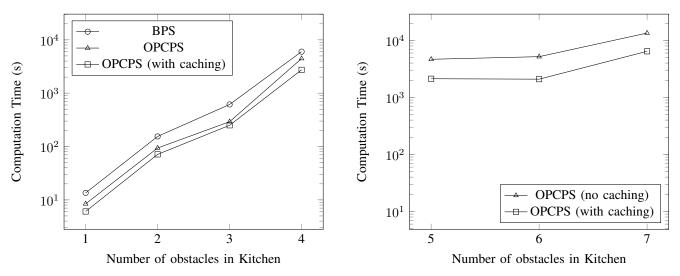


Fig. 9: Performance comparison between BPS, OPCPS with and without caching.

replanning is difficult, users can decrease the bound $\delta_{p_{replan}}$ and allocate computational resources for a high success rate.

Note that the replanning probability bound is a conservative upper bound of the failure rate since it pessimistically assumes all the uncovered observation branches that require replanning will fail, which is a rare case in practice. As we can see from Fig. 7, even with a high replanning probability bound $\delta_{p_{\text{replan}}} = 0.9$, the failure rate is at most 30%, which is much smaller than the given bound $\delta_{p_{\text{replan}}} = 0.9$.

C. Gains from Updating Replanning Probability Bound

As we discussed in Section IV-B, updating the replanning probability bound during partial conditional plan generation is important for avoiding unnecessary computation and improving efficiency. To evaluate the gains from this bound update step, we test OPCPS with and without the bound update in the kitchen domain with M = 4 obstacles.

Fig. 8a and 8b (semi-log scale) show the average replanning probability of the constructed partial conditional plans and the average total computation time as the bound $\delta_{p_{replan}}$ increases, respectively. As shown in Fig. 8a, with both settings (with and without the bound update) OPCPS constructs a partial conditional plan with a replanning probability smaller than

 $\delta_{p_{\text{replan}}}$. However, OPCPS without the bound update constructs a partial conditional plan with a lower replanning probability than that constructed by OPCPS with the bound update. Therefore, OPCPS without the bound update performs unnecessary computation and constructs a partial conditional plan with more branches and thus spends more time than OPCPS with the bound update, as shown in Fig. 8b. For the tests with $\delta_{p_{\text{replan}}} = 0.1, 0.2, 0.3$ that take more time to solve than those with $\delta_{p_{\text{replan}}} > 0.3$, OPCPS with the bound update achieves a 2-5 times speedup.

D. Gains from Caching

To evaluate the gains from caching, we compare the performance of OPCPS with caching against BPS and OPCPS without caching in the kitchen domain. For the kitchen domain with the number of obstacles ranging from 5 to 7, we compare results from OPCPS with and without caching only since BPS is not able to solve these problems within the time limit. We evaluated OPCPS with or without caching in the kitchen domain with different replanning probability thresholds. In Fig. 9, we present a complete benchmark for the performance evaluation of OPCPS with replanning probability bound $\delta_{p_{replan}} = 0.5$. We can see that OPCPS with caching performs much better compared

$\delta_{p_{replan}}$	Obstacle	Average Runtime (sec)		Worst-case Runtime (sec)	
		With Cache	Without Cache	With Cache	Without Cache
0.9	1	14	24	15	25
0.8	2	9	22	16	43
0.7	5	446	1047	1246	2863
0.6	6	2209	4031	3476	6015
0.7	7	1090	2542	2744	6001

TABLE I: A spot check for assessing performance gains from caching with different $\delta_{p_{replan}}$. The results showed that the performance of OPCPS is significantly improved with caching for both average and worst-case conditions. All results are averaged over 50 independent runs.

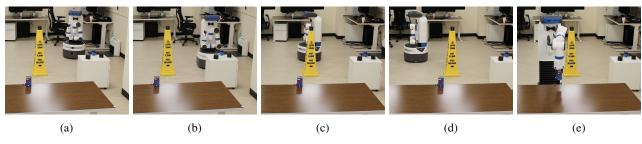


Fig. 10: Physical validation of OPCPS for the domain shown in Fig. 1.

to BPS and OPCPS. In fact, OPCPS with caching is 2.5 times faster on average. Our experimental results demonstrate that OPCPS with caching gains computational efficiency by reusing previously computed conditional plans.

However, it is often a question whether or not the better performance of OPCPS with caching holds with different replanning probability bounds $\delta_{p_{\text{replan}}}$. Because of the huge computational times involved (e.g., $\delta_{p_{\text{replan}}} = 0.7$ with 5, 6, 7 obstacles requires 72 - 96 CPU hours), we present a spot check in Table I for assessing performance gains from caching with different $\delta_{p_{\text{replan}}}$. From Table I, we observe similar trends for different replanning probability thresholds e.g., $\delta_{p_{\text{replan}}} = 0.9, 0.8, 0.7, 0.6$. Even when we choose a higher replanning probability, OPCPS with caching is 40% - 57% faster than OPCPS without caching both in average and worst-case runs.

E. Physical Validation

We conducted several physical validations using the mobile manipulator Fetch [45], which is equipped with a single 7-DOF arm, as well as a base-mounted laser scanner and a head-mounted 3D camera for perception. These validations were initially attempted in simulation using Gazebo [46], where the Fetch can be simulated over different environments. Both the simulated and the real-world robots are fully controlled via the Robot Operating System (ROS) [47]. The software control architecture of the robot includes a simultaneous localization and mapping (SLAM) system [48]. The SLAM utilizes the laser information to incrementally create a 2D map of the surroundings, which is used to provide a global localization of the robot [49]. For navigation purposes, the robot is equipped with a *move* action that takes the robot to a given position and orientation with respect to a global reference.

We validate OPCPS on the Fetch for the domain shown in Fig. 1. The setup is similar to the kitchen domain. The Fetch needs to pick up a target object (the blue can on the table) while avoiding collisions with uncertain obstacles such as floor signs and file cabinets, which can be placed in different locations. The POMDP's state space consists of locations of the robot and objects. We use the Vicon tracking system [50] to detect object locations, which is often accurate but can still produce false negative and false positive due to occlusion or inappropriate Vicon marker configurations on objects. We estimate the false negative and false positive probabilities by counting the false negative and false positive events during 100 Vicon detections. The POMDP's probabilistic observation function is defined based on the false negative and false positive probabilities.

To test the effects of different replanning probability bounds, we only allow the Fetch to move in three directions (west, east, and south), similar to the setup of the success rate experiments. Sometimes the Fetch may fail to move its base when given a *move* action command and stay in the same place. We estimate the failure probability of these move actions by counting the failure events during 100 *move* action executions. The POMDP's probabilistic transition function is defined based on this failure probability. Fig. 10a shows the initial state. There are two uncertain obstacles (a wet-floor sign and a file cabinet). We test OPCPS with two bounds $\delta_{p_{replan}} = 0.9$ and $\delta_{p_{replan}} = 0.1$.

With $\delta_{p_{\text{replan}}} = 0.9$, after observing no obstacle in the south direction, the Fetch decides to move south (Fig. 10b) because the partial conditional plan constructed with a high replanning probability bound does not cover the case where the Fetch is surrounded by obstacles and the wall. Then replanning fails but the Fetch still satisfies the safety requirement as shown in Fig. 10b, thanks to the safety guarantee provided by OPCPS.

However, with $\delta_{p_{\text{replan}}} = 0.1$, after observing no obstacles in the south direction, the Fetch decides to move west (Fig. 10c) because the partial conditional plan constructed with a low replanning probability bound covers the case where the robot is surrounded by obstacles. In order to avoid this situation, the Fetch needs to move west and gather more information. Then the Fetch observes an obstacle in the south direction and decides to move west again (Fig. 10d). Next, the Fetch observes no obstacle in the south direction, and now it can move south. Unlike the case shown in Fig. 10b where the robot is surrounded by two obstacles and the wall, in the situation shown in Fig. 10d, if there is another obstacle in the south



Fig. 11: Physical validation of OPCPS with caching for the lab domain. The Fetch requires to reach the table in (d) while avoiding white cabinets. The red rectangle in (a) and the blue rectangle in (d) represent the target and the start locations, respectively. The black line is the traversed path while following the policy generated by OPCPS with caching.

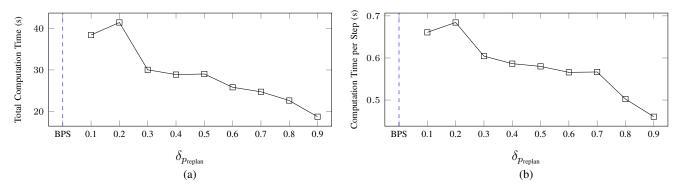


Fig. 12: Performance results for the Tag domain as the replanning probability bound $\delta_{P_{\text{replan}}}$ increases. All the results are averaged over 50 independent runs. Fig. 12a shows the average total computation time and Fig. 12b shows the average total computation time per step.

direction, the Fetch can still move west since there are only two obstacles. Finally, the Fetch moves to the table and picks up the target object (Fig. 10e).

We also validate OPCPS with caching on a Fetch robot in the same lab domain. The Fetch needs to reach a goal location while avoiding collisions with uncertain obstacles such as file cabinets. In this experiment, there are 2 uncertain obstacles (white cabinets) in the lab domain. The executions of the policy generated by OPCPS with caching are shown in Fig. 11a, 11b, 11c and 11d. As shown in the figures, the Fetch successfully reached the goal location (near the table in Fig. 11d) following the policy generated by OPCPS with caching. Our physical experiments show that the assumptions made in this work can correspond to realistic settings and that the behavior of the real robot is intuitive and correct.

F. Tag Domain

To further demonstrate the advantage of OPCPS over BPS, we evaluate OPCPS on a classic POMDP domain [3]. The task for the robot is to search for and tag a moving agent in a grid with 29 locations. The agent follows a fixed strategy that intentionally moves away from the robot. Both the robot and the agent can move in four directions or stay. The robot's location is fully observable while the agent's location is unobservable unless the robot and the agent are in the same location.

This Tag domain is challenging for BPS because of a large number of observations (|O| = 30) and more importantly, a huge planning horizon for computing a full conditional plan. However, computing a full conditional plan is unnecessary since replanning is easy in this domain. Fig. 12a and 12b show the average total computation time and the average computation time per step for the Tag domain as the bound $\delta_{p_{\text{replan}}}$ increases. These results show a similar trend to the previous kitchen domain tests: with a small bound $\delta_{p_{\text{replan}}} = 0.1$, we observe a big performance gain compared to BPS. BPS cannot solve this test within the 1800-second time limit while OPCPS with $\delta_{p_{\text{replan}}} = 0.1$ can solve this test in around 40 seconds and the computation time per step is less than 1 second. We also perform a spot check for assessing performance gains from caching in this domain as well. With $\delta_{p_{\text{replan}}} = 0.4$, we observe a significant performance gain compared to OPCPS without caching. In this setting, OPCPS without caching takes 658 seconds on average and 1541 seconds on average and 611 seconds on worst case to solve this test.

VI. DISCUSSION

We presented a new approach, called OPCPS, to policy synthesis for POMDPs with safe-reachability objectives. We introduce the notion of a *partial conditional plan* to improve computational efficiency. Rather than explicitly enumerating all possible observations to construct a *full* conditional plan, OPCPS samples a subset of all observations to ensure bounded replanning probability. Our theoretical and empirical results show that the failure rate of a valid partial conditional plan is bounded by the replanning probability. Moreover, OPCPS guarantees that the robot still satisfies the safety requirement when replanning fails. Compared to our previous BPS method [6], OPCPS with a proper replanning probability bound scales better in the tested domains and can solve problems that are beyond the capabilities of BPS within the time limit. The results also suggest that for domains where replanning is easy, increasing the replanning probability bound usually leads to better scalability, and for domains where replanning is difficult or impossible in some states, we can decrease the replanning probability bound and allocate more computation time to achieve a higher success rate. Our results also indicate that by updating the replanning probability bound during partial conditional plan generation, we can quickly detect if the current partial conditional plan satisfies the bound and avoid unnecessary computation. Moreover, compared to OPCPS without caching, OPCPS with caching reuses constructed partial conditional plans for sampled belief states and greatly improves the computational efficiency as shown in the results.

In this work, we focus on discrete POMDPs. While many robot applications can be modeled using this discrete representation, discretization often suffers from the curse of dimensionality. Investigating how to deal with continuous POMDPs [9], [10], [12], [21] directly is a promising future direction. OPCPS constructs partial conditional plans by sampling observations according to the probability of occurrence (Algorithm 3, line 44), which does not consider the importance of observations [14]. How to extend OPCPS to handle critical observations is another important ongoing question.

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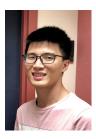
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